

# DECIMAL OPERATIONS 7

## MULTIPLYING DECIMALS

Multiply the numbers. Don't worry about the decimal points just yet.

$$\begin{array}{r} 1.124 \\ \times 1.5 \\ \hline 5620 \\ 1124 \\ \hline 16860 \end{array}$$

Count the total number of decimal places (or hops). In this case there are 3 on the top and one on the bottom.

$$\begin{array}{r} 1.124 \\ \times 1.5 \\ \hline 5620 \\ 1124 \\ \hline 16860 \end{array}$$

Place the decimal point in the answer. Use the same number of hops (decimal places) that you counted.

$$\begin{array}{r} 1.124 \\ \times 1.5 \\ \hline 5620 \\ 1124 \\ \hline 1.6860 \end{array}$$

**SHWOOPIE!**

## DIVIDING DECIMALS

Make the divisor a whole number by moving the decimal point to the right. Move the decimal point in the dividend by the same number of hops. This is the same as multiplying both numbers by 10 (for each hop.)

$$.2 \overline{)12.64}$$

$$2 \overline{)126.4}$$

Place the decimal point in the answer lined up with decimal point in the dividend.

$$2 \overline{)126.4}$$

Divide the numbers. Be sure that the decimal points remain lined up.

$$2 \overline{)126.4} = 63.2$$

### more examples

$$6.625 \div 0.53 \rightarrow 662.5 \div 53$$

$$\begin{array}{r} 2.6 \\ 65 \overline{)169.0} \\ -130 \\ \hline 390 \\ -390 \\ \hline 0 \end{array}$$

## ADDING AND SUBTRACTING DECIMALS

$$136.04 + 102.27 \rightarrow \begin{array}{r} 136.04 \\ +102.27 \\ \hline 238.31 \end{array}$$

Write in vertical column, aligning the decimal points.

Add each column, starting on right. Carry digits when needed.

$$2.37 - 0.031 \rightarrow \begin{array}{r} 2.3\overset{6}{7}0 \\ -0.031 \\ \hline 2.339 \end{array}$$

Write in vertical column, aligning the decimal points.

Subtract each column, starting on right and working left. Borrow as needed.

### more examples

$$5 - 0.85$$

4 9

$$\begin{array}{r} 5.00 \\ -0.85 \\ \hline 4.15 \end{array}$$

$$\begin{array}{r} 45.12 \\ +37.1 \\ \hline 82.22 \end{array}$$

# FRACTION BASICS

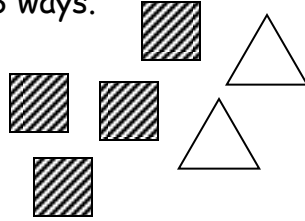
## RATIOS

**Ratio**- Compares two amounts or values; they can be written in 3 ways.

As a fraction  $\frac{2}{1}$

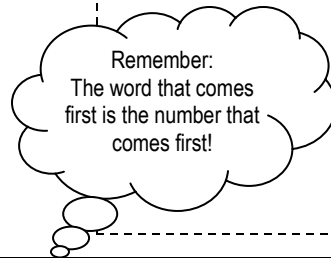
With a colon 2:1

With words "2 to 1"



**EXAMPLE:**

- Write the ratio of triangles to squares  
 $2:4$  (simplify to  $1:2$ )
- Write the ratio of total to squares  
 $6:2$  (simplify to  $3:1$ )



### RATIO WORD PROBLEM EXAMPLES:

A classroom has 15 girls and 10 boys.

- 1) What is the ratio of boys to total students?
- 2) What is the ratio of boys to girls?
- 3) What is the ratio of girls to boys?
- 4) What is the ratio of total students to girls?

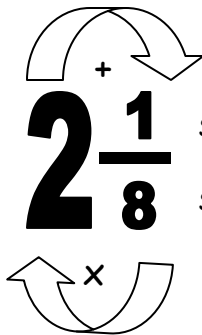
ANSWERS:  
1) 2:5  
2) 3:2  
3) 2:3  
4) 5:3

## IMPROPER FRACTIONS & MIXED NUMBERS

**Mixed number:** Whole number and a fraction

**Improper fraction:** numerator is greater than the denominator

### MIXED NUMBERS TO IMPROPER FRACTIONS



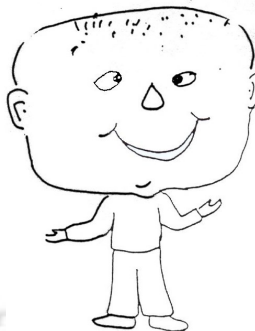
- STEP 1: Multiply the denominator times the whole number.  
STEP 2: Add your answer to the numerator.  
STEP 3: Put your number over your original denominator.

$$\frac{8 \times 2 + 1}{8} = \frac{17}{8}$$

Then add.



Multiply.



### IMPROPER FRACTIONS TO MIXED NUMBERS

$$\frac{25}{9}$$

STEP 1: Divide the numerator by the denominator.

STEP 2: Take the remainder and make it the numerator of a fraction with the divisor as the denominator.

$$9 \overline{)25} \begin{array}{r} 2 \text{ r}7 \\ -18 \\ \hline 7 \end{array}$$

$$9 \overline{)25} \begin{array}{r} 2 \text{ r}7 \\ -18 \\ \hline 7 \end{array}$$

$$2\frac{7}{9}$$

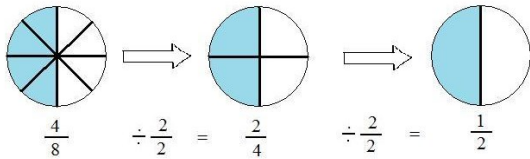
# FRACTION BASICS 9

## Fractions Bars

Use these fraction strips to find equivalent fractions.

ONE WHOLE																	
$\frac{1}{2}$								$\frac{1}{2}$									
$\frac{1}{4}$				$\frac{1}{4}$				$\frac{1}{4}$				$\frac{1}{4}$					
$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$		$\frac{1}{8}$			
$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$		
$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$		$\frac{1}{10}$			
$\frac{1}{5}$				$\frac{1}{5}$				$\frac{1}{5}$				$\frac{1}{5}$					
$\frac{1}{3}$						$\frac{1}{3}$						$\frac{1}{3}$					
$\frac{1}{6}$			$\frac{1}{6}$			$\frac{1}{6}$			$\frac{1}{6}$			$\frac{1}{6}$			$\frac{1}{6}$		
$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$		

## SIMPLIFYING FRACTIONS



When working with fractions, you need to write your answer in "simplest form." This means you need to simplify, or reduce, your fractions. At right, you can see that although the fraction  $\frac{1}{2}$  is written with smaller numbers, it still represents the fraction  $\frac{4}{8}$ .  $\frac{1}{2}$  is  $\frac{4}{8}$  the fraction written in simplest form.

One strategy for simplifying fractions is to check to see if you can simplify by 2, by 3, by 5, and by 7 (the first four prime numbers). See example at right.

Example: Simplify the fraction  $\frac{24}{108}$  :

$$\begin{array}{ccccccc}
 & \div 2 & & \div 2 & & \div 3 & \\
 & \curvearrowright & & \curvearrowright & & \curvearrowright & \\
 \frac{24}{108} & = & \frac{12}{54} & = & \frac{6}{27} & = & \frac{2}{9} \\
 & \curvearrowleft & & \curvearrowleft & & \curvearrowleft & \\
 & \div 2 & & \div 2 & & \div 3 & 
 \end{array}$$

# 10 MULTIPLYING FRACTIONS

## MULTIPLYING FRACTIONS

Multiply the numerators

$$\frac{2}{5} \times \frac{3}{4} = \frac{6}{20}$$

Multiply the denominators

$$\frac{2}{5} \times \frac{3}{4} = \frac{6}{20}$$

Reduce the fraction if necessary

$$\frac{6}{20} = \frac{3}{10}$$

- Multiply the numerators.
- Multiply the denominators.
- SIMPLIFY!

EXAMPLE:

$$\frac{3}{4} \times \frac{1}{2} = \frac{3 \times 1}{4 \times 2} = \frac{3}{8}$$

## MULTIPLYING MIXED NUMBERS

- Write mixed numbers as improper fractions.
- Put whole numbers over one
- Multiply the numerators.
- Multiply the denominators.
- SIMPLIFY! No improper fractions as an answer.

$$1\frac{2}{3} \times 4\frac{1}{2} =$$

$$\frac{5}{3} \times \frac{9}{2} = \frac{45}{6} = 7\frac{3}{6} \quad \left(7\frac{1}{2}\right)$$

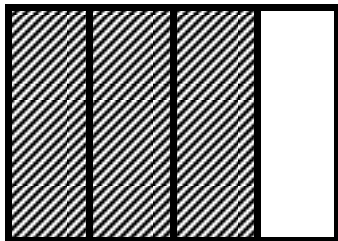
$$1\frac{2}{3} \times 4 =$$

$$\frac{5}{3} \times \frac{4}{1} = \frac{20}{3} \quad \left(6\frac{2}{3}\right)$$

Make  $1\frac{2}{3}$  improper by doing the "MA" circle.  
Make 4 improper, by putting  $\frac{4}{1}$ .

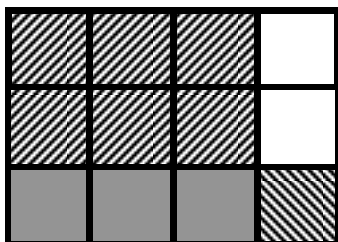
## MODELING MULTIPLYING FRACTIONS

Find  $\frac{1}{3}$  of  $\frac{3}{4}$  by modeling.



To find  $\frac{1}{3}$  of  $\frac{3}{4}$ , first draw  $\frac{3}{4}$  vertically.

Shade three-fourths.



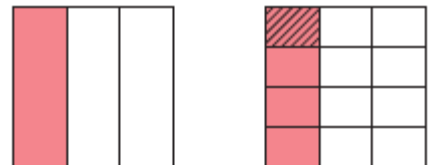
Then break the fourths into thirds horizontally.

Shade one-third.

The amount overlapping is the solution.

$$\frac{1}{3} \text{ of } \frac{3}{4} \text{ is } \frac{3}{12} \text{ or } \frac{1}{4}$$

Find  $\frac{1}{4}$  of  $\frac{1}{3}$ .



$$\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$$



# DIVIDING FRACTIONS 11

## DIVIDING FRACTIONS

Invert the fraction that you are dividing by

K C F  
 $\frac{4}{5} \div \frac{2}{3} = \frac{4}{5} \times \frac{3}{2}$

Multiply the numerators and denominators

$$\frac{4}{5} \times \frac{3}{2} = \frac{12}{10}$$

Simplify the fraction if necessary

$$\frac{12}{10} = 1\frac{1}{5}$$

K C F

$$\frac{1}{5} \div \frac{3}{8} =$$

KEEP the first fraction

CHANGE divide to multiply

FLIP the second fraction (reciprocal)

$$\frac{1}{5} \times \frac{8}{3} = \frac{8}{15}$$

## DIVIDING MIXED NUMBERS

- Write mixed numbers as improper fractions.
- Put whole numbers over one.
- KEEP the first fraction, CHANGE divide to multiply, FLIP the second fraction (reciprocal)
- Multiply the numerators.
- Multiply the denominators.
- SIMPLIFY! No improper fractions as an answer.

$1\frac{2}{3} \div 4\frac{1}{2} =$

K C F

$$\frac{5}{3} \div \frac{9}{2}$$

$$\frac{5}{3} \times \frac{2}{9} = \frac{10}{18}$$

$\frac{5}{9}$

Divide. Write each answer in simplest form.

**A**  $\frac{4}{5} \div 5$

$$\frac{4}{5} \div 5 = \frac{4}{5} \cdot \frac{1}{5}$$

$$= \frac{4 \cdot 1}{5 \cdot 5}$$

$$= \frac{4}{25}$$

**B**  $2\frac{2}{3} \div 1\frac{1}{6}$

$$2\frac{2}{3} \div 1\frac{1}{6} = \frac{8}{3} \div \frac{7}{6}$$

$$= \frac{8}{3} \cdot \frac{6}{7}$$

$$= \frac{8 \cdot 2}{\cancel{3} \cdot 7}$$

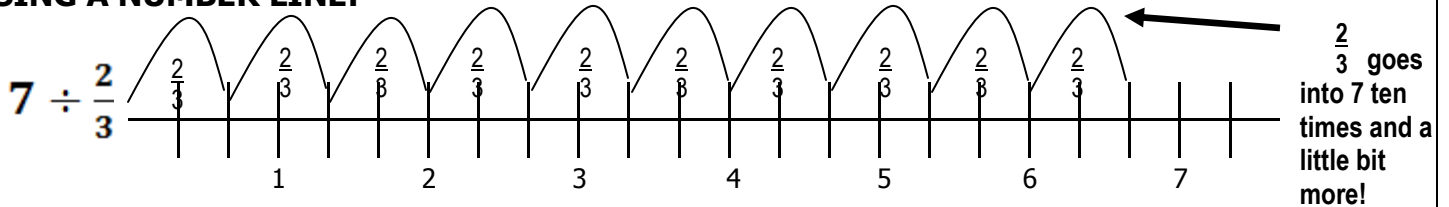
$$= \frac{16}{7}$$

$$= 2\frac{2}{7}$$



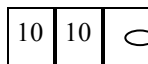
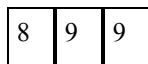
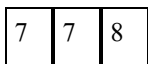
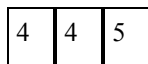
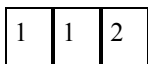
## MODELING DIVIDING FRACTIONS

USING A NUMBER LINE:



USING BARS:

$$7 \div \frac{2}{3}$$



Draw seven bars and divide them into thirds. Count off to see how many two-thirds are in 7 full bars. There are 10 two-thirds with some left over.



# SUBTRACTING FRACTIONS 13

## SUBTRACTING WITH UNLIKE DENOMINATORS

YOU MUST HAVE A COMMON DENOMINATOR FOR ADDING AND SUBTRACTING FRACTIONS.

### USING A RATIO TABLE

- Write both fractions in a table.
- Continue listing the multiples of the denominators until you find a common denominator.

FOR EXAMPLE:

$$\frac{3}{4} + \frac{3}{5} =$$

3				
4	8	12	16	20
3				
5	10	15	20	

So, 20 is the common denominator for  $1/4$  and  $3/5$

- Fill in the numerators on the table to find your fractions with a common denominator.

EXAMPLE CONTINUED:

3	6	9	12	15
4	8	12	16	20
3	6	9	12	
5	10	15	20	

- Add/subtract fractions.

EXAMPLE CONTINUED:

$$\frac{15}{20} - \frac{12}{20} = \frac{3}{20} = \frac{3 \div 5}{20 \div 5} = \frac{3}{4}$$

SIMPLIFY if you can!

### USING THE X---

- Find the LCM of the denominators and write at the end of the x---

$$\frac{2}{3} \times \frac{3}{3} = \frac{6}{9}$$

$$-\frac{4}{9} \times \frac{1}{1} = \frac{4}{9}$$

The common denominator for 3 and 9 is 9 (LCM)

- Find the LCM of the denominators and write at the end of the x---

$$\frac{2}{3} \times \frac{3}{3} = \frac{6}{9}$$

$$-\frac{4}{9} \times \frac{1}{1} = \frac{4}{9}$$

- Add or subtract

$$\frac{6}{9} - \frac{4}{9} = \frac{2}{9}$$

## SUBTRACTING FRACTIONS

- Get a common denominator and then subtract.
- If you have a fraction that you cannot subtract, then borrow!

4	5	1	2	3	4	16
	5	3	6	9	12	12
	2	10				10
		12				12

$4/12 - 10/12$  requires you to **BORROW**. Borrow from the whole number and add the denominator to the numerator of the top fraction (It's the same thing as adding one whole as  $12/12 + 4/12 = 16/12$ )

SIMPLIFY!  $\frac{2 \frac{6}{12}}{12} = \frac{2 \frac{1}{2}}{2}$

$$8 - 5\frac{3}{4} =$$

### Borrowing from a WHOLE NUMBER

$$\begin{array}{r} 8 - 5\frac{3}{4} \\ \underline{-5\frac{3}{4}} \quad \underline{-5\frac{3}{4}} \\ 2\frac{1}{4} \end{array}$$

Write 8 as a mixed number with a denominator of 4. Regroup 8 as  $7 + \frac{4}{4}$ . Subtract the fractions and then the whole numbers.

### OR DRAW the problem!



$$2\frac{1}{4}$$

Draw 8 circles. Shade in  $5\frac{3}{4}$ . The amount left unshaded is your answer.

# FRACTIONS-DECIMALS-PERCENTS

## DECIMAL

Divide the numerator by the denominator. When there is nothing left to bring down, add a decimal and zero.

$$\begin{array}{r} 0.125 \\ 8 \overline{)1.000} \\ \underline{-8} \phantom{00} \\ 20 \phantom{0} \\ \underline{-16} \phantom{0} \\ 40 \\ \underline{-40} \end{array}$$

Convert to

$$\frac{1}{8}$$

Fraction

## PERCENTAGE

1. Divide numerator by denominator

$$\begin{array}{r} 0.125 \\ 8 \overline{)1.000} \end{array}$$

2. Multiply answer by 100 and add a percent sign

$$0.175 \times 100 = 17.5\%$$

Or "SHWOOPIE" move the decimal two places to the right

## PERCENTAGE

Multiply by 100 and add a percent sign

or

"SWOOPIE" move the decimal two places to the right

Convert to

0.125

Decimal

## FRACTION

1. Remove decimal point and write the number as the numerator.

.125

2. The denominator is a multiple of 10, depending on the place value of the last digit

1000

3. Write the fraction and reduce to the lowest terms

$$\frac{125}{1000} = \frac{25}{200} = \frac{1}{8}$$

## FRACTION

1. Divide the percentage by 100 and drop the percent sign.

$$12.5\% = .125$$

Or

SHWOOPIE two steps to the left

2. Write the decimal as a fraction and reduce it to lowest terms

$$\frac{125}{1000} = \frac{1}{8}$$

Convert to

12.5%

Percentage

## DECIMAL

1. Divide the percentage by 100 and drop the percent sign.

$$12.5\% = .125$$

Or "Swoopie" two decimal places to the left



# fractions

- To turn a FRACTION into a DECIMAL, DIVIDE.
- Which number goes in the house? NUMERATOR
- No REMAINDERS.
- When you have nothing to bring down, add a DECIMAL and a ZERO!

FRACTION TO DECIMAL EXAMPLES:

$\frac{1}{5}$ $\begin{array}{r} 0.2 \\ 5 \overline{)1.0} \\ \underline{-0} \\ 10 \\ \underline{-10} \\ 0 \end{array}$	$\frac{3}{8}$ $\begin{array}{r} 0.375 \\ 8 \overline{)3.000} \\ \underline{-0} \\ 30 \\ \underline{-24} \\ 60 \\ \underline{-56} \\ 40 \\ \underline{-40} \\ 0 \end{array}$	$\frac{1}{9}$ $\begin{array}{r} 0.11111 \\ 9 \overline{)1.00000} \\ \underline{-0} \\ 10 \\ \underline{-9} \\ 10 \\ \underline{-9} \\ 10 \\ \underline{-9} \\ 1 \end{array}$
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To write a FRACTION as a PERCENT, first turn it into a decimal, then move the decimal 2 times to the right.

## the number cycle

### decimals

- To turn a DECIMAL into a PERCENT, move the DECIMAL two times to the RIGHT.

EXAMPLES:

$$0.72 = 72 \%$$

$$0.124 = 12.4 \%$$

$$1.34 = 134 \%$$

- To write a DECIMAL as a FRACTION write the number over its place value.

EXAMPLES:

$$0.23 = \frac{23}{100} \qquad 0.7 = \frac{7}{10}$$

### percents

- To turn a PERCENT into a DECIMAL, move the DECIMAL two times to the LEFT.

EXAMPLES:

$$50\% = 0.50$$

$$6\% = 0.06$$

$$200\% = 2.00$$

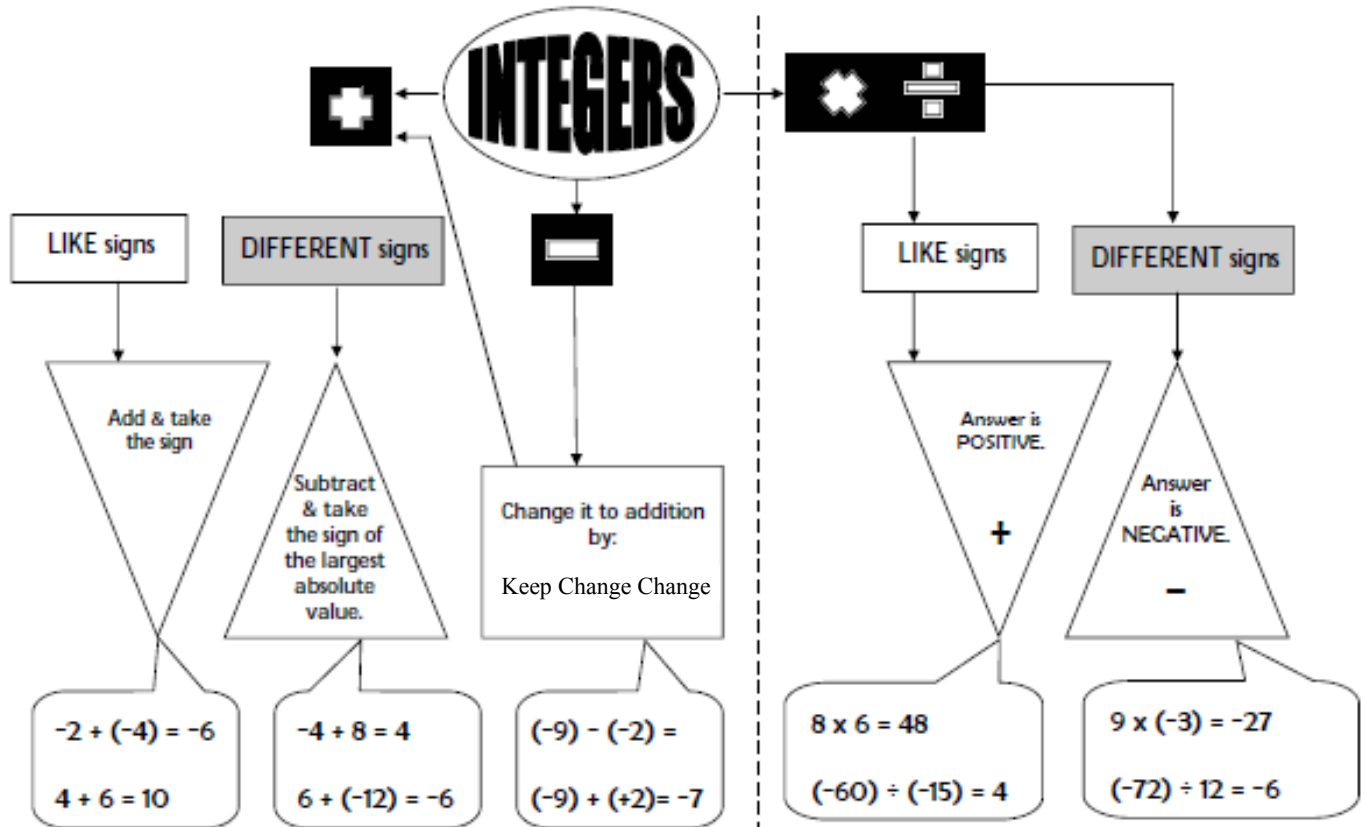
- To write a PERCENT as a FRACTION write it over 100, because percent means "out of 100."

EXAMPLES:

$$26\% = \frac{26}{100} = \frac{13}{50} \qquad 5\% = \frac{5}{100} = \frac{1}{20}$$

# INTEGER RULES <sup>21</sup>

## RULES FOR OPERATIONS



FOUND AT <http://www.sw-georgia.resa.k12.ga.us/integer%20rules.pdf>

## ADDING INTEGERS

**Same Sign: Add and keep the sign**

$$2 + 2 = 4$$

Positive + Positive = Positive

$$(-2) + (-2) = (-4)$$

Negative + Negative = Negative

**Different Signs: Subtract and keep the sign of the larger value (from zero)**

$$(-9) + 2 = (-7)$$

Big Negative + Small Positive = Negative

$$(-2) + 9 = 7$$

Small Negative + Big Positive = Positive

## MULTIPLYING AND DIVIDING INTEGERS

Positive x Positive = Positive

Negative x Negative = Positive

Negative x Positive = Negative

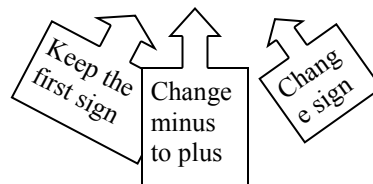
Positive x Negative = Negative

Division (same pattern)

## SUBTRACTING INTEGERS

Subtracting a negative is like ADDING A POSITIVE!

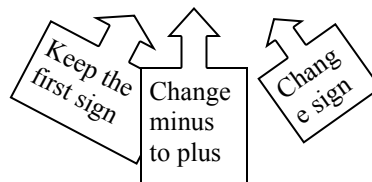
$$\begin{array}{r} 2 - (-2) = \\ 2 + 2 = 4 \end{array}$$



**KEEP  
CHANGE  
CHANGE**

Subtracting a positive IS subtracting or like ADDING A NEGATIVE!

$$\begin{array}{r} -8 - 4 = \\ -8 + (-4) = -12 \end{array}$$



Subtracting Integers

Subtraction is the same as **adding the opposite**, so rewrite subtraction problems as addition problems and then use addition rules.

$$\begin{array}{l} -6 - 3 = -6 + -3 = -9 \\ 4 - -9 = 4 + 9 = 13 \\ 2 - 7 = 2 + -7 = -5 \end{array}$$